

# Borrowing an Identity for a Distributed Counter

[Work in progress report]

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MSc Student at University of Minho  
PaPoC '17, Belgrade

1. Distributed Counters
2. Building CRDTs
3. Borrow-Counter

# Distributed Counters

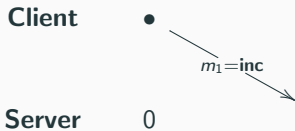
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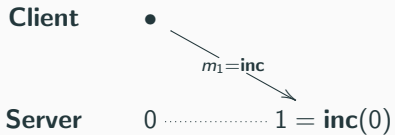
**Client**

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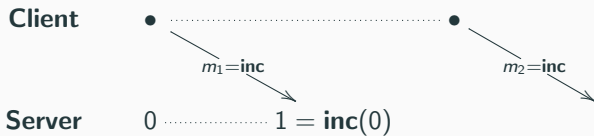
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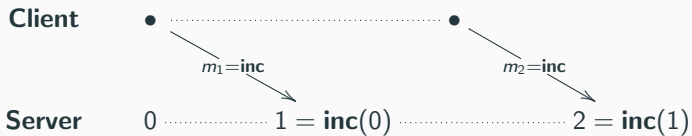
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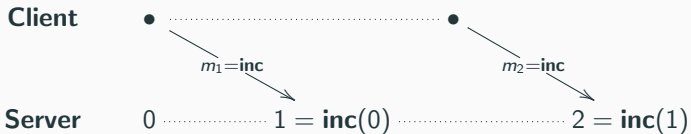


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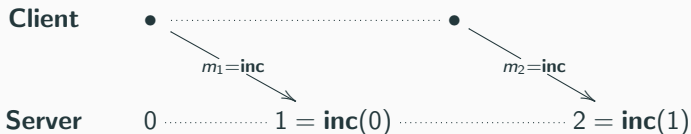


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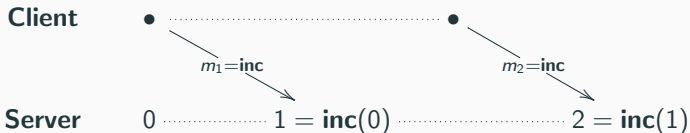
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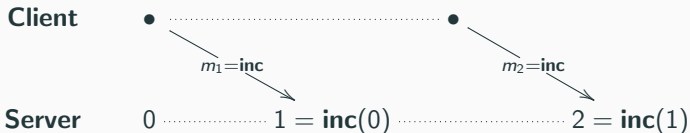


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(See CASSANDRA-2495: Add a proper retry mechanism for counters in case of failed request)

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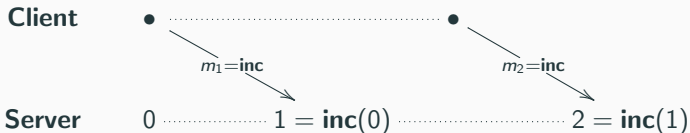
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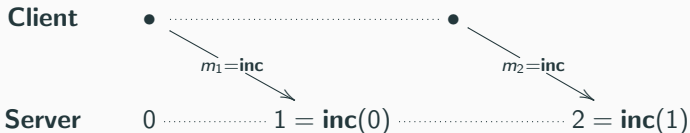


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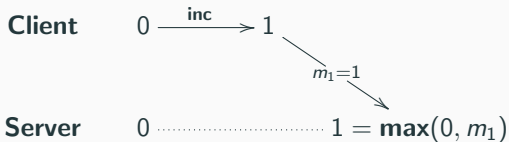


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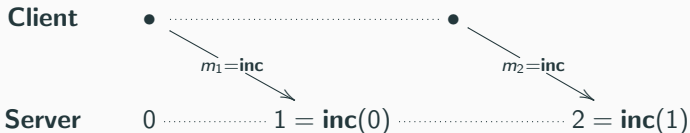


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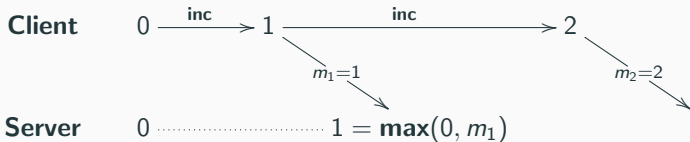


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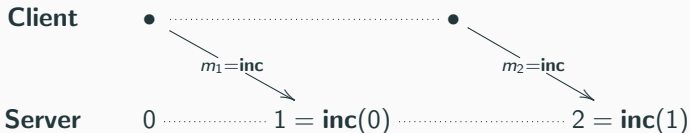


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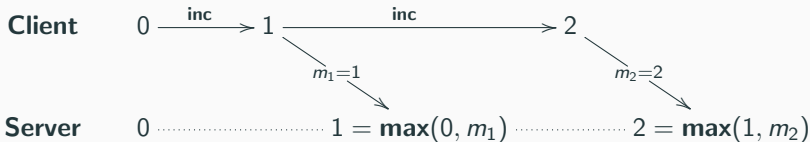


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**Is it solved? Can I leave?**

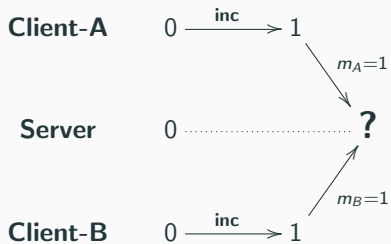
## Let's make it more interesting

Client-A    0  $\xrightarrow{\text{inc}}$  1

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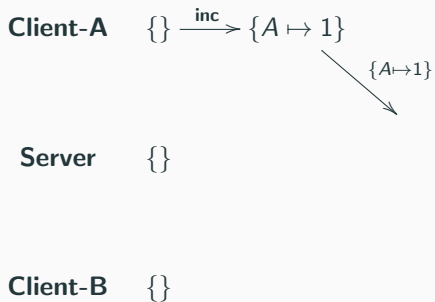
# Naming CRDTs: GCounter

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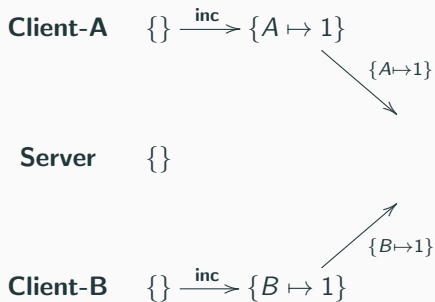
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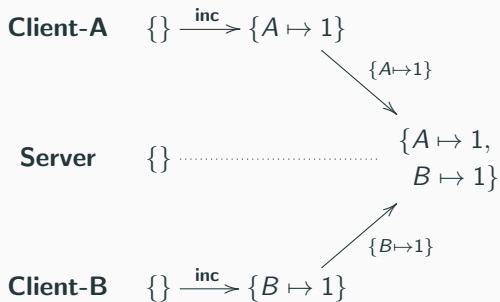




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- Safe **retirement** transient of nodes, incorporating their increments in a permanent node

# Building CRDTs

---

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✓  $\{\}$

✓  $\{A \mapsto 2, B \mapsto 1\}$



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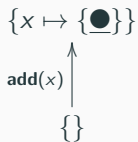
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- $\mathcal{D} = \{\bullet, \blacktriangle, \blacksquare\}$  (for now)

**AWS**et $\langle \mathcal{E} \rangle = \mathcal{E} \hookrightarrow \mathcal{P}(\mathcal{D} \times \mathbb{B})$   
(with tombstones)

$\{\}$

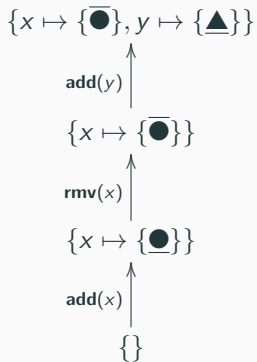
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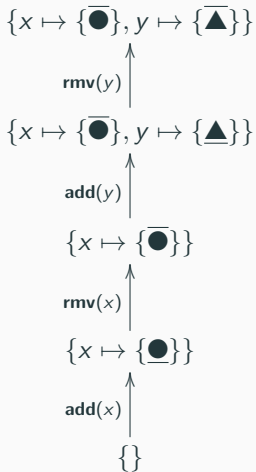


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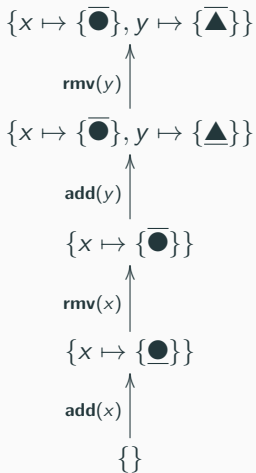


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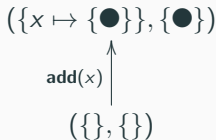
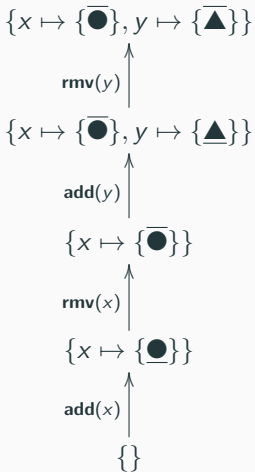
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$(\{\}, \{\})$

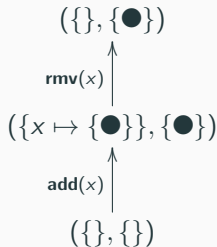
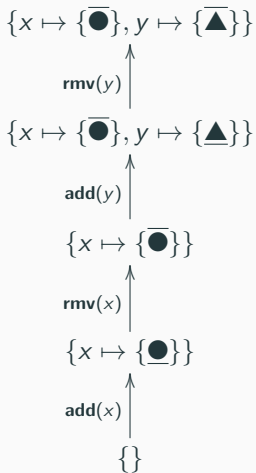
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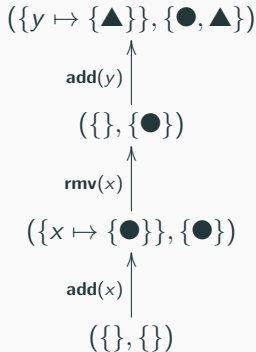
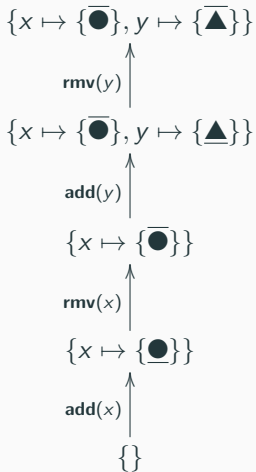
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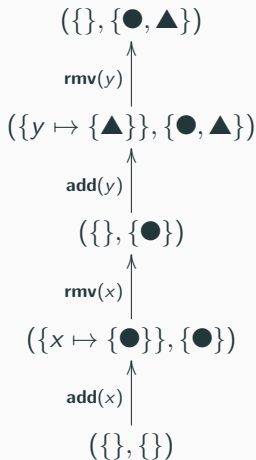
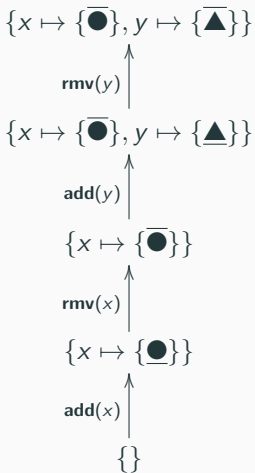
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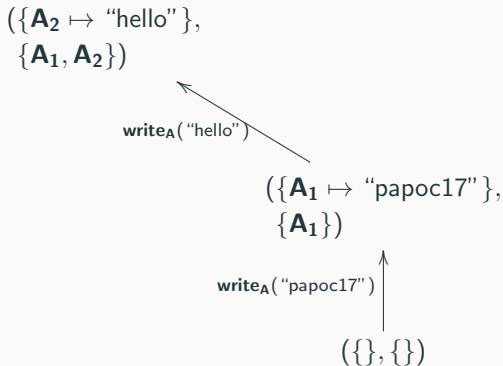
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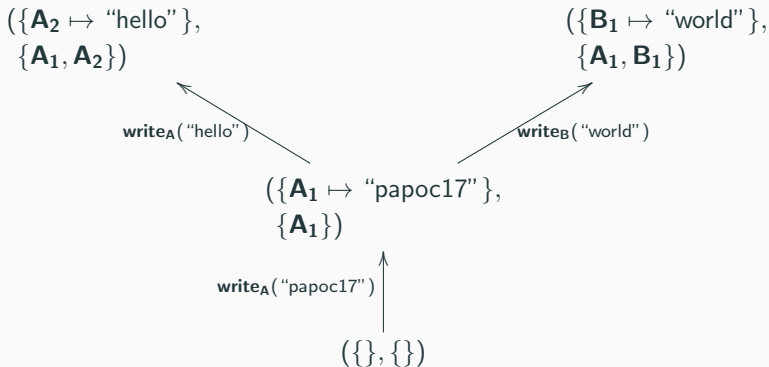
$$\begin{array}{c} (\{\mathbf{A}_1 \mapsto \text{"papoc17"}\}, \\ \{\mathbf{A}_1\}) \\ \uparrow \text{write}_{\mathbf{A}}(\text{"papoc17"}) \\ (\{\}, \{\}) \end{array}$$

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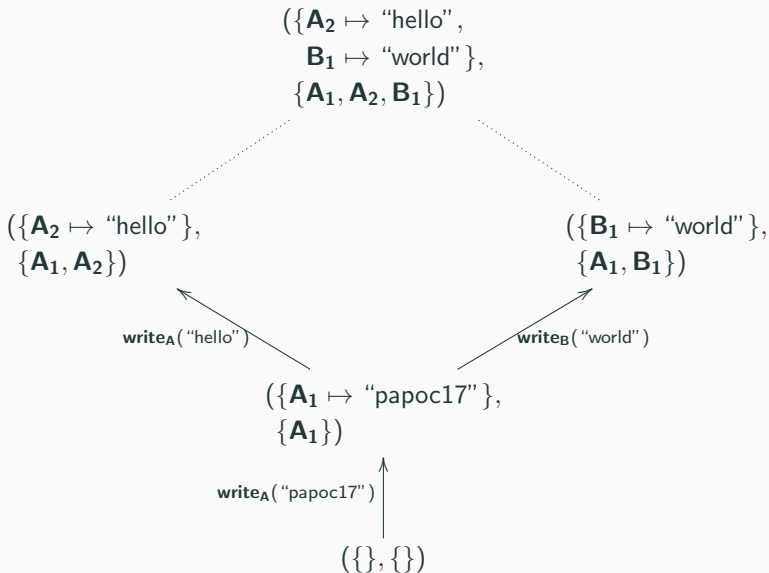


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- What about dot ownership?



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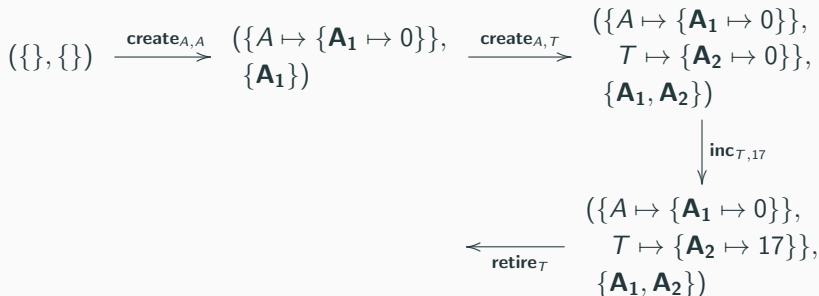
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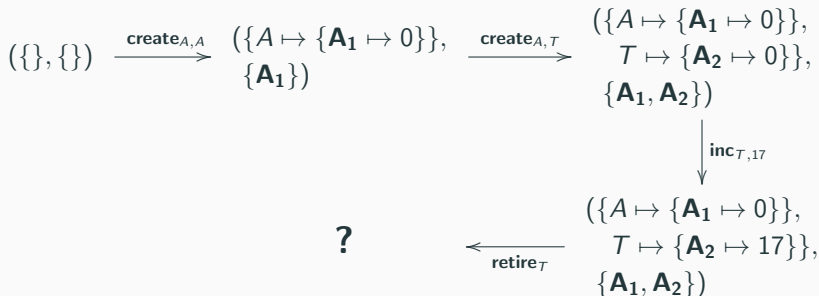
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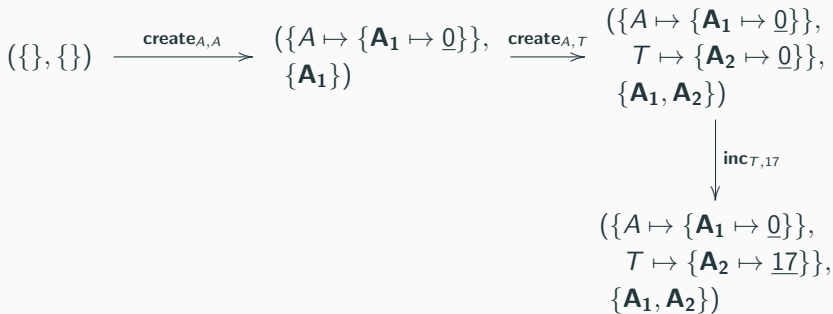
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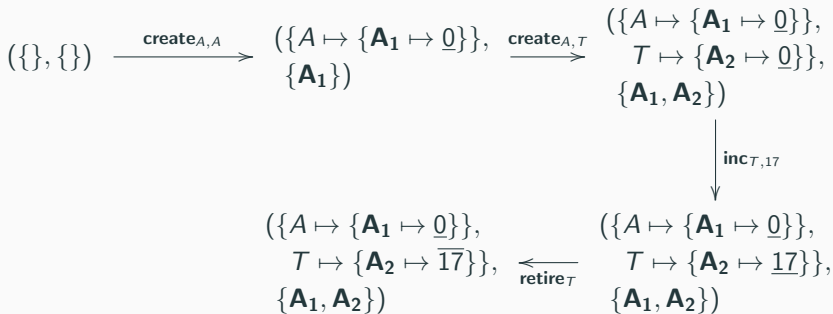
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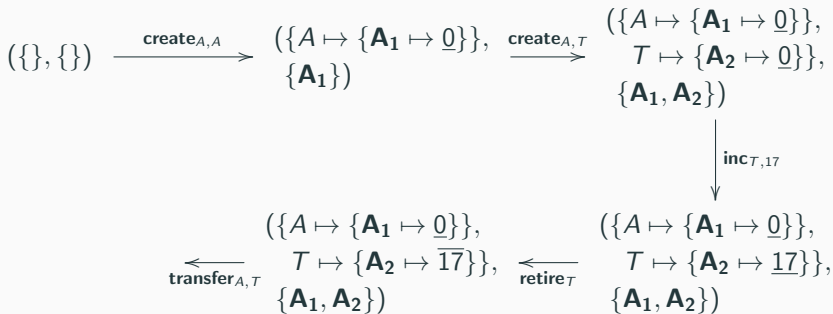
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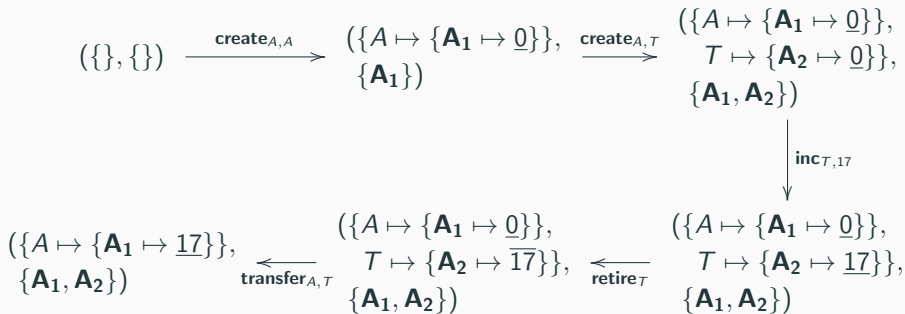




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# What we covered

- The Identity Explosion Problem
- CRDT building techniques
- **Borrow-Counter**: a new design for CRDT counters that allows retirement of transient nodes
  - (We focused on increment-only counters)

# Questions?

[bit.ly/borrow-papoc](https://bit.ly/borrow-papoc)